

Asymptotes of Rational Functions

Vertical:

For the equation $f(x) = \frac{n(x)}{d(x)}$ the vertical asymptote occurs when $d(x) = 0$

Horizontal:

When the degree of the polynomial is the same in the numerator and

denominator, such as $f(x) = \frac{ax^2+bx+c}{tx^2+ux+v}$, the horizontal asymptote occurs at $y = \frac{a}{t}$

When the degree of the polynomial in the numerator is less than the

denominator, such as $f(x) = \frac{ax+b}{tx^2+ux+v}$, the horizontal asymptote occurs at $y = 0$

Oblique/Slant:

When the degree of the polynomial in the numerator is greater than the

denominator, such as $f(x) = \frac{ax^2+bx+c}{ux+v}$, use long division or synthetic division to

find the oblique/slant asymptote